

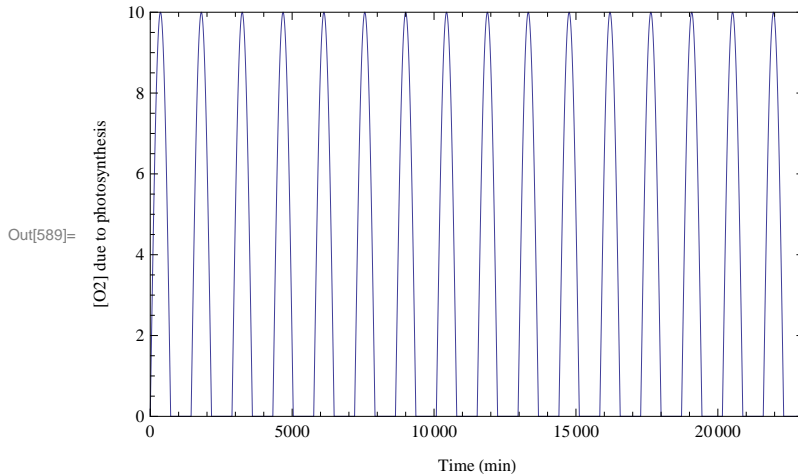
## ■ Photosynthetic Sine Wave

```
In[2]:= sine[A_, F_, PSI_, time_, D_] := Module[{recov, trunk},
  recov = A * N[Sin[(2 * Pi * F * time + PSI)]] + D];
```

```
#####Test of sine wave over 16 days (23,040 min)#####
```

```
In[3]:= gt = Map[sine[10, .00069444444444444445, 0, #, 0] &, Table[i, {i, 1, 23 040}]];
gt2 = Map[If[# ≤ 0, 0, #] &, gt];
```

```
In[589]:= ListLinePlot[gt2, PlotRange → {{0, 23 040}, {0, 10}}, Frame → True,
  FrameLabel -> {"Time (min)", "[O2] due to photosynthesis"}]
```



## ■ Biological Oxygen Demand (BOD) curve

```
In[7]:= BOD[prey_, h_] := Module[{shit},
  shit = 1 + 10 * (prey / (prey + h));
  shit]
```

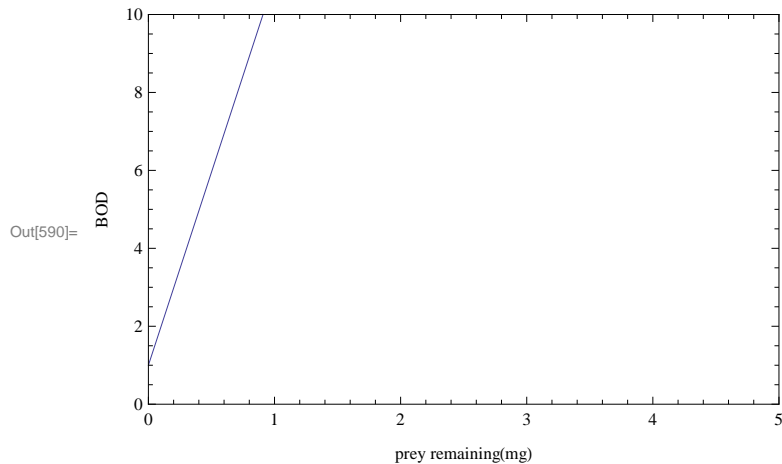
```
#####Test of BOD curve#####
```

```
In[420]:= curve = Map[BOD[#, .01] &, Table[i, {i, 0, 5}]]
```

```
Out[420]= {1., 10.901, 10.9502, 10.9668, 10.9751, 10.98}
```

```
In[422]:= coupled = Partition[Riffle[Table[i, {i, 0, 10}], curve], 2];
```

```
In[590]:= ListLinePlot[coupled, PlotRange -> {{0, 5}, {0, 10}},
  Frame -> True, FrameLabel -> {"prey remaining(mg)", "BOD"}]
```



### ■ Prey Consumption Curve

```
In[16]:= pcurve[a_, b_, t_] := Module[{curve},
  curve = a * E^(-b * t)]
```

####The solution function solves pcurve for any prey (chew) value####

```
In[17]:= solutionFunction[chew_, day_] := Round[N[t /. Solve[pcurve[20, 4, t] == chew]] * day]
```

```
In[20]:= Round[N[t /. Solve[pcurve[20, 4, t] == 1]] [[1]] * 1440]
```

Out[20]= 1078

```
In[591]:= Testpcurve =
```

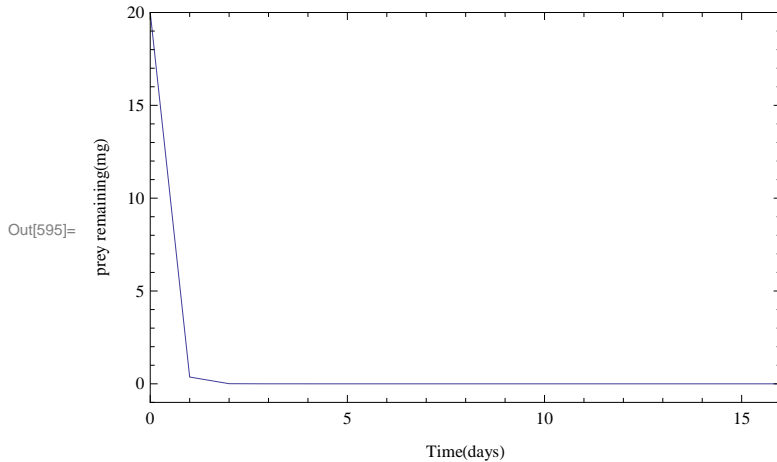
```
N[Map[pcurve[20, 4, #] &, {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16}]]
```

Out[591]= {20., 0.366313, 0.00670925, 0.000122884, 2.2507 × 10<sup>-6</sup>, 4.12231 × 10<sup>-8</sup>, 7.55027 × 10<sup>-10</sup>,  
1.38288 × 10<sup>-11</sup>, 2.53283 × 10<sup>-13</sup>, 4.63905 × 10<sup>-15</sup>, 8.49671 × 10<sup>-17</sup>, 1.55623 × 10<sup>-18</sup>,  
2.85033 × 10<sup>-20</sup>, 5.22056 × 10<sup>-22</sup>, 9.56179 × 10<sup>-24</sup>, 1.7513 × 10<sup>-25</sup>, 3.20762 × 10<sup>-27</sup>}

```
In[592]:= coup = Partition[
```

```
Riffle[{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16}, Testpcurve], 2];
```

```
In[595]:= ListLinePlot[coup, PlotRange -> {{0, 16}, {-1, 20}},
  Frame -> True, FrameLabel -> {"Time(days)", "prey remaining(mg)"}]
```



### ■ Nitrogen as a function of prey and oxygen

```
In[35]:= Nitrogen[prey_, oxygen_] := Module[{N},
  N = oxygen * prey / 100]
```

```
#####For low oxygen levels [O2]=1#####
```

```
In[36]:= one = Map[Nitrogen[#, 10] &, {0, .1, .2, .3, .4, .5, .6, .7, .8, .9, 1}]
```

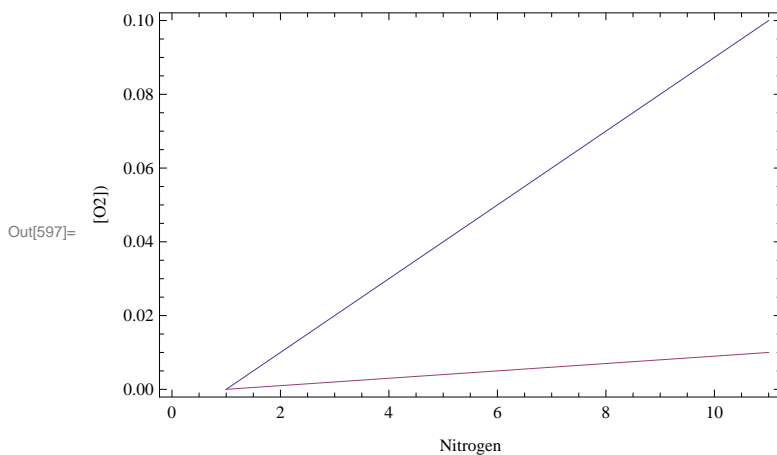
Out[36]=  $\left\{0, 0.01, 0.02, 0.03, 0.04, 0.05, 0.06, 0.07, 0.08, 0.09, \frac{1}{10}\right\}$

```
#####For high oxygen levels [O2]=9#####
```

```
In[37]:= nine = Map[Nitrogen[#, 1] &, {0, .1, .2, .3, .4, .5, .6, .7, .8, .9, 1}]
```

Out[37]=  $\left\{0, 0.001, 0.002, 0.003, 0.004, 0.005, 0.006, 0.007, 0.008, 0.009, \frac{1}{100}\right\}$

```
In[597]:= ListLinePlot[{one, nine}, Frame -> True, FrameLabel -> {"Nitrogen", "[O2]"}]
```



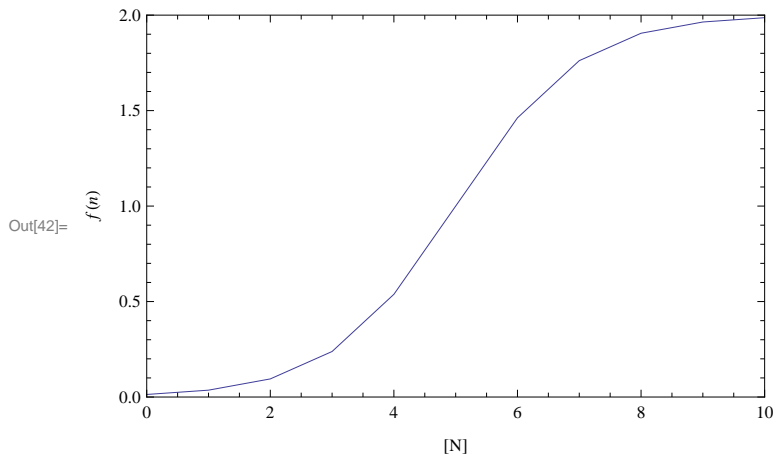
### ■ Oxygen augmentation to the sine curve as a function of mineralized N

```
In[39]:= sig[MO_, MX_, a_, x_, d_] := Module[{one, two, three},
  one = a (x - d);
  two = N[E^one];
  three = (MO) + ((MX - MO) / (1 + two));
  three]
```

```
In[40]:= feedback = Map[sig[0, 2, -1, #, 5] &, {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10}];
```

```
In[41]:= coupled = Partition[Riffle[{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10}, feedback], 2];
```

```
In[42]:= ListLinePlot[coupled, PlotRange -> {{0, 10}, {0, 2}},
  Frame -> True, FrameLabel -> {"[N]", "f(n)"}]
```



```
#####Augmentation Function#####
```

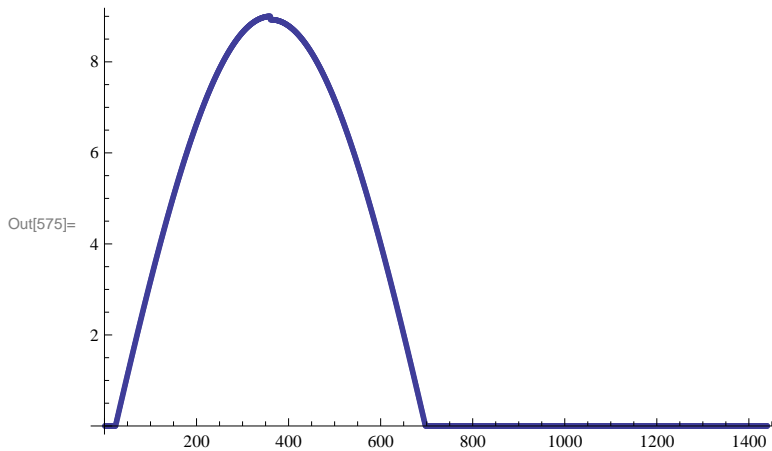
```
Aug[prey_, oxy_] := Module[{Aug, N},
  N = Nitrogen[prey, oxy];
  Aug = sig[0, 2, -1, N, 5];
  Aug]
```

### ■ Dynamics of entire model for 1 day (1440 min)

```
In[573]:= Day[{previousChow_, preyloss_, previousSpot_, prevO2_}, addchow_, lastday_, h_,
  Aug_, b_] := Module[{index, o2, newChow, sin, nullsin, bod, remove, nullo2,
  tfake, curveTime2, curveTime, t, chew, left, BigcurveTime, ppChow2},
  index = previousSpot + 1;
  sin = sine[10 * Aug, .0006944444444444445, 0, index, 0];
  nullsin = If[sin ≤ 0, 0, sin];
  ppChow2 = If[index == 360, addchow + previousChow, previousChow];
  BigcurveTime =
  If[index < 360, Round[N[t /. Solve[pcurve[20, b, t] == lastday]][[1]] * 1440],
  Round[N[t /. Solve[pcurve[20, b, t] == addchow + lastday]][[1]] * 1440]];
  tfake = If[ppChow2 == 0, BigcurveTime, BigcurveTime + index];
  remove = N[pcurve[20, b, BigcurveTime * 0.0006944444444444445]] -
  N[pcurve[20, b, tfake * 0.0006944444444444445]];
  left = If[remove == 0, ppChow2, pcurve[20, b, tfake * 0.0006944444444444445]];
  bod = BOD[left, h];
  o2 = nullsin - bod;
  nullo2 = If[o2 < 0, 0, o2];
  {left, remove, index, nullo2}]

In[574]:= O2Dynamics = NestList[Day[#, .1, 0, 5, 1, 4] &,
  {0, 0, 0, sine[10 * 1, .0006944444444444445, 0, 0, 0]}, 1439];

In[575]:= or = ListPlot[Map[#[[4]] &, O2Dynamics]]
```



### ■ Looping theDynamics for all 16 days

```
In[576]:= dayPlus[{Augment_, old_, lastday_}, addchow_, b_] :=
  Module[{O2Dynamics, outs, aug, finalO2, nchow, leftoverChow},
  O2Dynamics = NestList[Day[#, addchow, lastday, .1, Augment, b] &,
  {lastday, 0, 0, sine[10 * Augment, .0006944444444444445, 0, 0, 0]}, 1439];
  outs = O2Dynamics[[All, {1, 2, 4}]];
  finalO2 = outs[[1440]][[3]];
  nchow = outs[[1440]][[2]];
  leftoverChow = outs[[1440]][[1]];
  aug = Aug[nchow, finalO2] + Augment;
  {aug, outs, leftoverChow}]
```

```
In[578]:= run = NestList[dayPlus[#, 5, 4] &, {1, 1, 0}, 16];
```

### ■ Process data and plot

```
In[581]:= fr = Partition[Flatten[Map[run[[#]] [[2]] &, Table[i, {i, 2, 17}]]], 3];
```

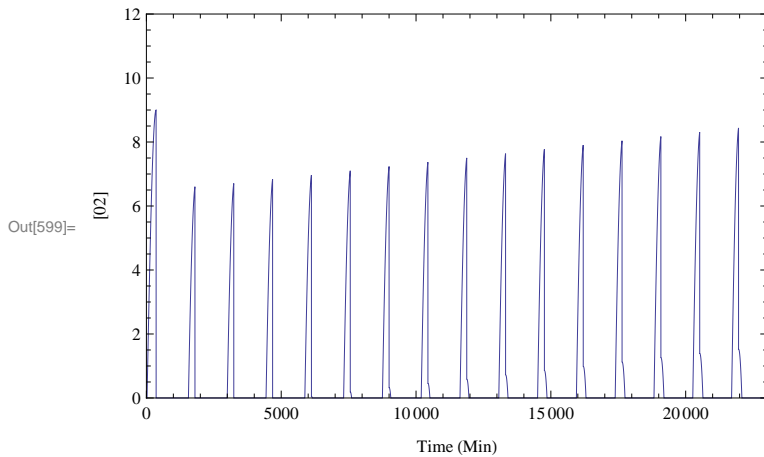
```
In[582]:= Dimensions[fr]
```

```
Out[582]:= {23 040, 3}
```

```
In[583]:= wchow = Map[#[[1]] &, fr];
```

```
In[598]:= o2 = Map[#[[3]] &, fr];
```

```
In[599]:= ListLinePlot[o2, PlotRange -> {{0, 23 040}, {0, 12}},  
Frame -> True, FrameLabel -> {"Time (Min)", "[02]"}]
```



```
In[600]:= ListLinePlot[wchow, PlotRange -> {{0, 23 500}, {0, 20}},  
Frame -> True, FrameLabel -> {"Time (Min)", "Prey Remaining (mg)"}]
```

